The Elliptical Cone of Uncertainty in Diffusion Tensor Imaging and Its Normalized Measures

C. Koay¹, and P. J. Basser¹
¹National Institutes of Health, Bethesda, MD, United States

INTRODUCTION
The diffusion tensor is always measured in the presence of background noise. Recent experimental observations by Jeong et al.[1] and Lazar et al.[2,3] have shown that the cones of uncertainty (COU) [4,5,6] of the major eigenvectors of the diffusion tensors in the brain are mostly elliptical. Analytical approaches have also been developed to characterize the elliptical cone of uncertainty [7] through nonlinear least squares estimations [8]. Here, we present a new technique to construct the COU based on the inverse of the Gnomonic projection and two normalized geometric measures associated with the COU—the normalized areal and circumferential measures.

METHODS
A simple closed or Jordan curve [9] on the unit sphere divides the unit sphere into two regions. If the simple closed curve is not the great circle then one region will be greater than the other. The normalized areal measure is the ratio of the area of the smaller region on the unit sphere, which is enclosed by a simple closed curve whose Gnomonic (or central) projection [10] on the Cartesian plane is an ellipse as depicted in Figure 1A, to the area of the hemisphere. The ratio of the circumference of the simple closed curve on the unit sphere to the circumference of the great circle of the unit sphere is the normalized circumferential measure. The inverse of the Gnomonic projection is used to construct the proposed COU, Figure 1B, that avoids overlapping cones in neighboring regions.

RESULTS AND DISCUSSION
Simulated human brain diffusion tensor data were used to generate the normalized areal measure map, Fig 2A, and the normalized circumferential measure map, Fig 2B. The simulated data were generated from a single tensor model at an SNR level of 15. The normalized maps were computed from the 0.95 joint confidence region (or 95% confidence region), of the COU. Figure 3 shows the COUs of an axial slice of the simulated human brain using the proposed technique.

The normalized circumferential and areal measures are local parametric coherence measures for quantifying tract dispersion. The key advantage of the proposed measures for quantifying uncertainty of the major eigenvector of the diffusion tensor is that these measures are dimensionless and normalized to unity. Further, they have direct geometric interpretations.

Since the major eigenvector of the diffusion tensor is usually associated with the directional preference of the diffusing water molecules. The proposed measures, which are directly linked to the uncertainty in the major eigenvector of the diffusion tensor, may be important for probing the integrity of the white matter tracts in the brain and for assessing the quality and reliability of DTI tractography [11-15].

REFERENCES