

## Pore diameter mapping using double pulsed-field gradient MRI and its validation using a novel glass capillary array phantom

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### ABSTRACT

Double pulsed-field gradient (d-PFG) MRI can provide quantitative maps of microstructural quantities and features within porous media and tissues. We propose and describe a novel MRI phantom, consisting of wafers of highly ordered glass capillary arrays (GCA), and its use to validate and calibrate a d-PFG MRI method to measure and map the local pore diameter. Specifically, we employ d-PFG Spin-Echo Filtered MRI in conjunction with a recently introduced theoretical framework, to estimate a mean pore diameter in each voxel within the imaging volume. This simulation scheme accounts for all diffusion and imaging gradients within the diffusion weighted MRI (DWI) sequence, and admits the violation of the short gradient pulse approximation. These diameter maps agree well with pore sizes measured using both optical microscopy and single PFG diffraction NMR spectroscopy using the same phantom. Pixel-by-pixel analysis shows that the local pore diameter can be mapped precisely and accurately within a specimen using d-PFG MRI.

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### 1. Introduction

There is a growing need for accurately measuring salient microstructural features in turbid samples and specimens non-invasively and *in situ* in fields ranging from materials science and oil exploration to radiology. New diffusion MRI methods can address this need and can fill an important niche in characterizing microstructures on microscopic and macroscopic length scales.

Most diffusion MRI methods employ the single pulsed-field gradient (PFG) MR sequence [1] in which the spins' net displacements are encoded using a pair of magnetic field gradient pulses, and the resulting signal attenuation profile (due to the spins dephasing

during the time between those pulses) can be used to infer microstructural features or dimensions of the porous medium [2].

In biological and clinical applications, for instance, diffusion tensor MRI (DTI) [3,4] is a widely used method to obtain information about tissue anisotropy and fiber orientation. It entails acquiring PFG MRI scans obtained with multiple gradient orientations and/or gradient strengths, producing Diffusion Weighted Images (DWIs). While diffusion is assumed to be Gaussian in DTI, more explicit models of water diffusion in nerve tissues, such as those assumed in CHARMED [5] and in AxCaliber MRI [6], allow one to estimate more detailed microstructural features of neural tissue, such as their intra- and extra-axonal volumes, and the mean axon diameter, or in the case of AxCaliber, the axon diameter distribution within a single voxel.

PFG MR is effective in measuring compartment or pore dimensions in uniform, highly ordered media [7–11] from well-defined diffraction peaks they produce. However due to the inverse

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relationship between the pore diameter and the scattering vector,  $q = (2\pi)^{-1}\gamma G\delta$ , a large  $q$ -value ( $q = |\mathbf{q}|$ ) is required to obtain fine-scale information about pore size. Typically, such high  $q$ -values are not achievable in animals or clinical MRI scanners [12]. Generally, in biological and clinical applications, one cannot even observe the first null point of the diffraction spectrum in microporous structures owing to the high  $q$ -values needed. Furthermore, in heterogeneous porous specimens that have a polydisperse distribution of pore diameters or pore shapes [13] these diffraction peaks [14] quickly disappear. Such is also the case in neural tissue.

Double pulsed-field gradient (d-PFG) MRI methods, however, have the potential to overcome many of the deficiencies and limitations of PFG MRI detecting features of complex tissue microstructure, below the resolution of the MRI voxel [15–19], not detectable by PFG MRI. Multiple-PFG MR sequences are constructed by concatenating two or more PFG MR sequences. This enables one to observe or measure correlations between net displacements of spins during multiple diffusion periods, from which one can infer a number of fine-scale features. For instance, by varying the mixing time  $\tau_m$  – the time between the PFG blocks—different microstructural parameters can be extracted. For the measurement of pore size or fiber diameter little or no mixing time is required, while for the detection of local anisotropy a long mixing time is used [15,20–23].

Previously, pore diameters in packs of beads, radish [17], spinal cord [17,24], and corticospinal tissue [25,26] have been measured using d-PFG MRI techniques. Although numerical phantoms were used in some of these studies [24,27] to ensure that reasonable pore sizes were measured, these methods and models were not validated or calibrated experimentally using well-characterized physical MRI phantom with known pore sizes. Furthermore, d-PFG MRI data are likely to suffer from bias introduced by the cross-terms from the imaging gradients themselves, and between imaging and diffusion gradients. Finally, the use of the short pulse approximation can greatly simplify the form of the model relating the MR signal decay, the d-PFG sequence, and pore dimensions. However, due to the scanner limitations the MR sequences in many cases do not satisfy the short pulse approximation, complicating the analysis of the d-PFG MRI data.

In this study we used a d-PFG filtered MRI sequence (Fig. 1) to measure and map average pore diameters of new MRI phantom. We also describe the development and use of this new MRI phan-

tom, which is suitable to calibrate and validate MRI pore mapping experiments. The phantom consists of a glass capillary array (GCA) with a known monodisperse pore diameter distribution, which was measured and cross-validated using optical light microscopy and single PFG NMR spectroscopy diffraction experiments [28]. A recently introduced theoretical framework [29] was employed for estimating pore size wherein all imaging and diffusion gradient waveforms were taken into account, and the long diffusion pulses that violate the short pulse approximation, were explicitly accounted for. A spatially resolved map of local pore diameters was then created pixel-by-pixel by analysis of the d-PFG images of this novel MRI phantom.

## 2. Materials and methods

Fig. 2a and b shows a photographic enlargement and microscopic image, respectively, of the GCA MRI phantom. The phantom consists of two lead glass GCA wafers (Photonis, Sturbridge, MA) 13 mm OD, each containing a pack or array of microcapillaries with a nominal pore diameter of 10  $\mu\text{m}$  (and a 5% maximum pore size variation between GCAs). The capillary arrays were filled with pure water using a three-step procedure. First, water vapor was adsorbed on the internal walls of the capillaries. This was achieved by exposing the GCAs to water vapor of controlled activity (isopiestic method). The water activity (relative vapor pressure) was kept below 0.95 to avoid droplet and bubble formation in the capillaries. Second, water activity was gradually increased in the vapor phase to fill the capillaries by condensation. Third, the GCA was immersed in an excess amount of water to ensure complete filling and then placed in a 15 mm NMR tube (New Era Enterprises Inc., Vineland, NJ). The phantom was inserted into the magnet's bore with the long axis of the capillaries aligned with the direction of the main magnetic field.

The d-PFG MRI sequence used in this study consisted of two PFG spin-echo NMR blocks concatenated together, followed by a spin-echo MRI block (Fig. 1). In this implementation, the d-PFG NMR blocks can be viewed as a “filter” that selects a subset of the spins for the subsequent MRI sequence. The RF pulses used in the filter were all short, hard broadband pulses in order to reduce possible additional echoes resulting from imperfect pulses: however phase cycling schemes or adiabatic rf pulses can be used if such echoes arise. The mixing time,  $\tau_m$ , defined as the time between the two

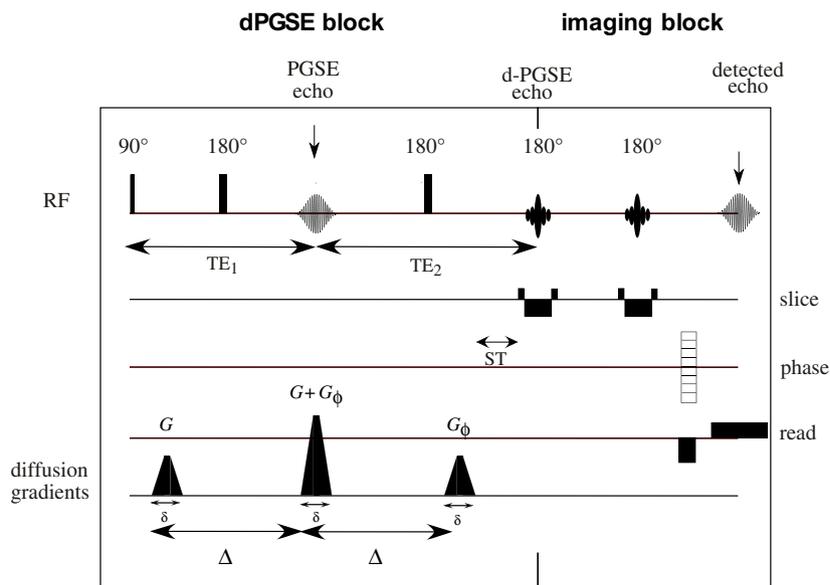
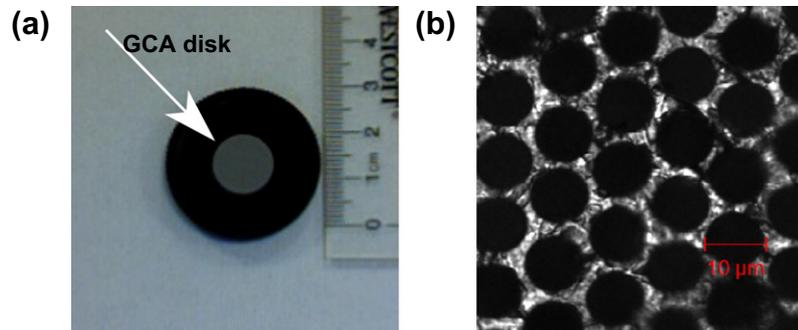


Fig. 1. The d-PFG MRI pulse sequence used in this study.



**Fig. 2.** (a) The glass capillary array (Photonis, Sturbridge, MA) with 13 mm disk diameter, 10  $\mu\text{m}$  nominal pore diameter and 500  $\mu\text{m}$  thickness. (b) Confocal transmission image of the GCA showing a 10  $\mu\text{m}$  pore diameter.

PFG blocks, was zero, which resulted in a superposition of the second gradient pulse of the first PFG block and the first gradient pulse of the second PFG block. The angle between the  $x$  PFG block,  $\phi$ , was varied between  $0^\circ$  and  $360^\circ$  in  $45^\circ$  increments in the  $XY$  plane—the plane whose normal vector lies parallel to the GCA's tubes' axes. When the gradients in the two PFG blocks are parallel ( $\phi = 0$ ), the middle gradient pulse is doubled in strength; when the two PFG blocks are anti-parallel ( $\phi = 180^\circ$ ) the middle gradient pulse vanishes. All other angles result in different combinations of  $X$  and  $Y$  gradients. The MRI block in this implementation consisted of two slice selective refocusing rf pulses, which yields  $T_2$  weighted images with an independent TE. This block, however, is interchangeable and can be replaced with other imaging blocks to suit the sample requirements, (e.g., a fast imaging block for *in vivo* measurements).

All experiments were performed on a 7T vertical Bruker wide-bore DRX MRI system (Bruker BioSpin, Germany) equipped with a Micro2.5 microimaging probe and three GREAT60 gradient amplifiers having a nominal peak current of 60 A per channel. This configuration can produce a maximum nominal gradient strength of  $24.65 \text{ mT m}^{-1} \text{ A}^{-1}$  along each of the three orthogonal directions. Sample temperature was set at  $19^\circ\text{C}$ .

The sequence was first calibrated on a water sample using PFG NMR parameters: gradient pulse duration (including the gradient ramp time) ( $\delta$ ) = 3.15 ms, diffusion time ( $\Delta$ ) = 50 ms, and gradient strength ( $G_1 = G_2$ ) = 0, 44, 74 and  $103 \text{ mT m}^{-1}$  resulting in  $q = 5.9, 9.9$  and  $13.8 \text{ mm}^{-1}$ ; and MRI parameters: repetition time (TR) = 7000 ms, echo time of the imaging block (TE) = 20 ms, field of view (FOV) = 10 mm and slice thickness = 2 mm. The number of averages (NA) = 2, total acquisition time was 30 min. Gradients stability was tested on an isotropic sample of 5 cSt of polydimethylsiloxane (PDMS), which has a diffusivity of about an order of magnitude smaller than free water. The PFG NMR parameters were:  $\delta = 3.15$  ms;  $\Delta = 50$  ms; and ( $G_1 = G_2$ ) = 0, 74, 147, 221 and  $295 \text{ mT m}^{-1}$ . Resulting in  $q = 9.9, 19.8, 29.7$  and  $39.6 \text{ mm}^{-1}$ . The MRI parameters were: TR = 7000 ms; TE = 12 ms; FOV = 10 mm; and slice thickness = 1 mm. NA = 2, total acquisition time was 30 min.

Analytical calculations were carried out for the echo attenuation,  $E(G_1, G_2, \phi)$ , for each  $\phi$  used between the two PFG blocks. The expression for free isotropic diffusion is given by [18]:

$$E = e^{-\gamma^2 D_0 \delta^2 \left[ \left(1 - \frac{\delta}{\Delta}\right) (G_1^2 + G_2^2) - \left(\frac{\delta}{\Delta}\right) G_1 G_2 \cos \phi \right]} \quad (1)$$

where  $\gamma$  is the proton's magnetogyric ratio and  $D_0$  is the diffusion coefficient of the solvent within the tubes. We used  $D_0 = 1.98 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$  for water at  $19^\circ\text{C}$  [30].

The d-PFG MRI experiments were then performed on the GCA phantom. The PFG NMR parameters were:  $\delta = 3.15$  ms;  $\Delta = 50$  ms; and ( $G_1 = G_2$ ) = 0, 74, 147, 221, and  $295 \text{ mT m}^{-1}$ . Resulting in  $q = 9.9, 19.8, 29.7$ , and  $39.6 \text{ mm}^{-1}$ . The MRI parameters were:

TR = 7000 ms; TE = 12 ms; FOV = 20 mm; and slice thickness = 1 mm (which covers both GCA disks). NA = 4, total acquisition time was 60 min. To evaluate whether the separation time (ST) between diffusion and imaging gradients affected the pore diameter estimations, experiments were performed using two different d-PFG filters having different ST, a short time of 1.3 ms and a long time of 20.8 ms. One would expect short ST to affect pore diameter estimation for restricted geometries where the last diffusion gradient would not refocus the magnetization. Therefore the spins might not lose their coherence before the imaging gradients are applied. To ensure that the imaging block did not affect the d-PFG echo attenuation, experiments were repeated with a long TE of 70 ms and ST of 20.8 ms. Measurements of the echo intensity were performed using a Region of Interest (ROI) in the center of the image to avoid artifacts arising from Gibbs ringing [31]. The ROIs, which were taken, included the macroscopic defects; however, those were incorporated into the free diffusion component of the simulations. To create the pore diameter maps, a pixel-by-pixel analysis was performed: each pixel's intensity for all 38 gradient configurations (nine angles with four gradient strengths and two non-diffusion weighted MRIs) was used to estimate the pore diameter in each voxel.

To validate the d-PFG MRI results, images of the GCAs used in the phantom were taken on a Zeiss LSM 510 inverted laser-scanning microscope (Carl Zeiss, Jena, Germany). The dry phantoms were deposited in an Attofluor chamber (Invitrogen, Carlsbad, CA) with a number 1.5 coverslip at the bottom and imaged with a  $20 \times 0.75$  NA plan-apochromat (dry) Zeiss objective in transmission mode using differential interference contrast (DIC) settings. Images were recorded at maximum resolution ( $2048 \times 2048$  pixels), which yields a spatial resolution of  $0.22 \mu\text{m}$  per pixel, at zoom 1 with 3% transmission of the 488 nm laser line and no averaging. Under these conditions, the glass substrate appeared bright while the core of each capillary was dark. Accurate spatial calibration was obtained by imaging a calibrated ruler (Graticules LTD., Tonbridge, England) in both the horizontal and vertical orientation. Images were analyzed in Metamorph software (Molecular Devices, Downingtown, PA) by first calibrating in  $x$  and  $y$ , then thresholding the image to isolate the capillary cores. The images were then binarized, submitted to one cycle of erosion and dilation to remove stray pixels and measured with the Integrated Morphometry Analysis drop-in. The equivalent diameter, the diameter of a circle that would contain an area equal to that of the object, was retained as the most reliable measurement of the capillary pore size. Particles of less than  $7.5 \mu\text{m}$  and more than  $15 \mu\text{m}$  diameter were discarded as they represent either objects not adequately resolved by thresholding or contacting the image border. At least 10 images were recorded at different locations of each phantom, and the results averaged.

PFG NMR diffusion-diffraction experiments were also performed on the same GCA phantom. These were conducted using a stimulated echo (STE) PFG NMR sequence with the following

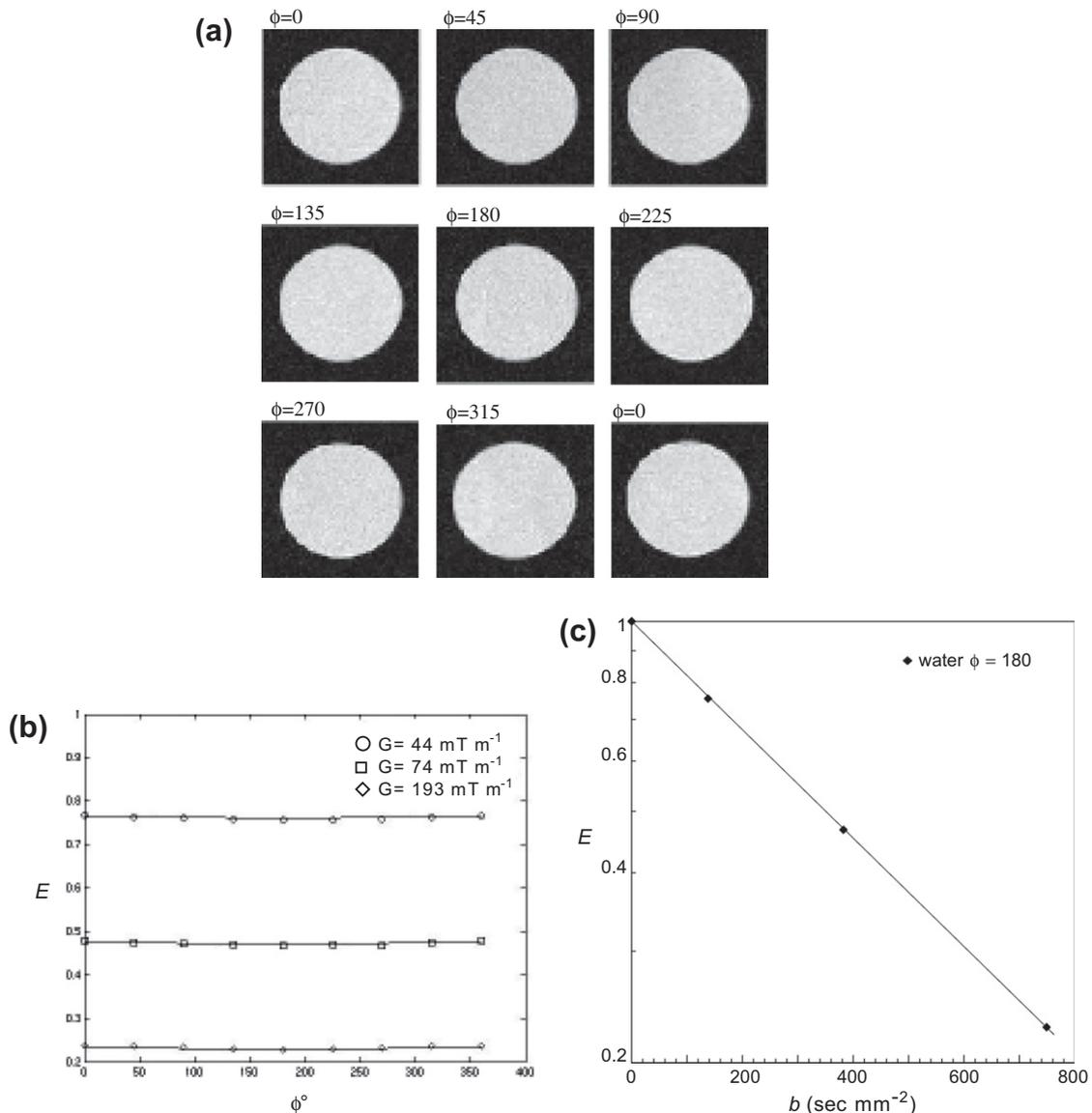
parameters:  $\delta = 4$  ms,  $\Delta = 250$  ms and 32  $q$ -values were collected with  $G_{\max} = 1200$  mT m<sup>-1</sup>, resulting in a  $q_{\max}$  of 204.3 mm<sup>-1</sup>.

To examine and interpret our experimental data and provide a method to infer or estimate pore size from both PFG NMR and d-PFG MRI experiments, we employed a matrix operator formalism to predict  $E(q, \phi)$  (where  $q = \gamma G \delta / (2\pi)$ ) for diffusion within a restricted cylinder. Our method generalizes and extends previous work to model the effects of long diffusion gradient pulses on  $E(q)$  data obtained in PFG NMR experiments in various well defined restricted geometries (e.g., within spheres, cylinders, and between parallel plates). To this end, Caprihan et al. (27) and Callaghan (28) approximated an arbitrary gradient waveform by a train of impulses leading to the multiple propagator approach. An alternative and computationally efficient approach involves expressing a general gradient waveform as a series of step functions, as was done in Refs. [32,33]. However, these works have assumed that the gradient orientation remained fixed throughout the acquisition, which is clearly violated in the general d-PFG acquisitions and in all MRI sequences. To circumvent this shortcoming, Özarlan et al. recently introduced a general framework that accounts for the vari-

ations in the gradient orientation [29], in which each pulse of the sequence was represented with a vector operator whose components were infinite-dimensional matrices. An operator obtained by exponentiating the corresponding matrix expresses the effect of each interval in the pulse sequence on the magnetization. This approach enables one to write, with relative ease, an analytical expression for the MR signal intensity, which is exact for piecewise continuous gradient waveforms, and can be used to obtain a very good approximation for other pulse sequences. The details of the approach are outside the scope of this paper, and can be found in [29]. In this work, we employed this technique by, respectively, incorporating and ignoring the imaging gradients of the d-PFG NMR filtered pulse sequence illustrated in Fig. 1. The presence of a small free water compartment was also incorporated in these calculations [18,28].

### 3. Results

Fig. 2b shows a typical confocal transmission image of a small FOV of a GCA. Measurements of the two GCA wafers that we used



**Fig. 3.** (a) d-PFG MRI images of free water using  $\delta = 3.15$  ms,  $\Delta = 50$  ms and  $G = 44$  mT m<sup>-1</sup>. The angle between the gradient directions of each PFG block is specified in the left corner of each image. (b) Experiments and simulations of the corresponding echo attenuations vs.  $\phi$  for  $G = 0, 44, 74$  and  $103$  mT m<sup>-1</sup>. (c) Echo attenuation at  $\phi = 180$  vs.  $b = (2\pi)^2 q(\Delta - \delta/3)$  (mm<sup>-1</sup>).

to construct the phantom yielded an average pore diameter of  $9.5 \pm 0.2 \mu\text{m}$  and  $9.4 \mu\text{m} \pm 0.2 \mu\text{m}$ .

The first model system we used to test our d-PFG MRI was an isotropic water sample. Fig. 3a shows d-PFG MRI images of water for the nine different  $\phi$  using a gradient strength of  $44 \text{ mT m}^{-1}$  (where artifacts originating from RF inhomogeneity were expected). All images were free of any observable systematic artifacts or distortion. The SNR ranged from 41 for  $G=0$  to 10 for  $G=103 \text{ mT m}^{-1}$ . Fig. 3b shows the echo attenuation of the water at  $\phi = 180$  vs. the  $b$ -value,  $b = (2\pi)^2 q^2 (2\Delta - \delta/3)$ . The diffusion coefficient for free water that was calculated from that fit ( $D_0 = 1.97 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ ) agreed with the value used in the simulations ( $D_0 = 1.98 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ ). Fig. 3c shows the measured echo attenuation data,  $E(q, \phi)$  vs.  $\phi$ , (for  $G = 44, 74,$  and  $103 \text{ mT m}^{-1}$ , corresponding to  $q = 5.9, 9.9,$  and  $13.8 \text{ mm}^{-1}$ ). Superposed are predictions of  $E(q, \phi)$  vs  $\phi$  assuming free diffusion obtained using Eq. (1). Agreement between the experimental data and theory was excellent. As expected, for free isotropic (Gaussian) diffusion, a slight angular dependence of  $E(q, \phi)$  is observed. Also, as expected, as gradient strength or  $q$  was increased, signal attenuation increased. No observable artifacts were detected in the PDMS sample at all gradient strengths and  $E(q, \phi)$  vs.  $\phi$  curves agreed with the analytical calculations predicted by Eq. (1) (data not shown).

Next we applied our d-PFG MRI sequence to the GCA phantom. Fig. 4 shows d-PFG MRI data of the GCA for all nine  $\phi$  for  $G = 295 \text{ mT m}^{-1}$ . All images taken with the phantom were also free of observable artifacts. The dark streaks visible across the disk are macroscopic defects, which were also visible on spin and gradient-echo MRI scans (data not shown).

Fig. 5 shows experimental and simulated data superposed for all gradient strengths and  $\phi$  values used in this study. Specifically, Fig. 5a–c shows the data and fits for the various combinations of short and long STs, and TEs (ST = 1.3 ms TE = 12 ms, ST = 20.8 ms TE = 12 ms, and ST = 20.8 ms TE = 70 ms) experiments, respectively. The simulations based on the theory fitted the experimental data very well.

Fig. 6a–c shows pore diameter maps for short ST and short TE, long ST and short TE, and long ST and long ST experiments, respectively; Fig. 6d–f shows maps of the corresponding standard deviations for each pore diameter map. The images appear very similar

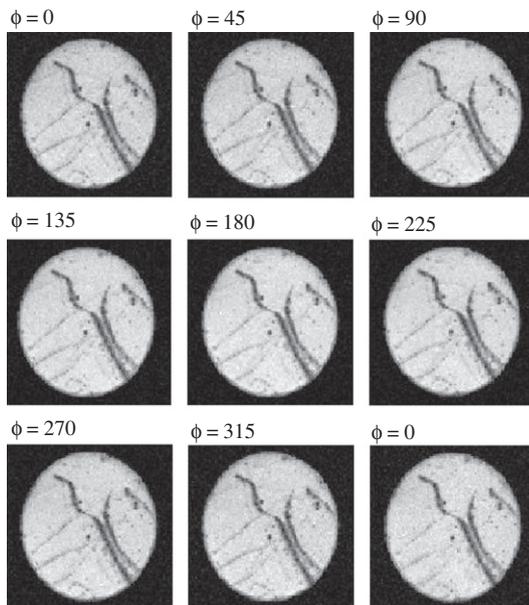


Fig. 4. d-PFG MRI images of the GCA phantom using  $\delta = 3.15 \text{ ms}$ ,  $\Delta = 50 \text{ ms}$ , and  $G = 295 \text{ mT m}^{-1}$ . The angle between the gradient directions of each PFG block is specified in the left corner of each image.

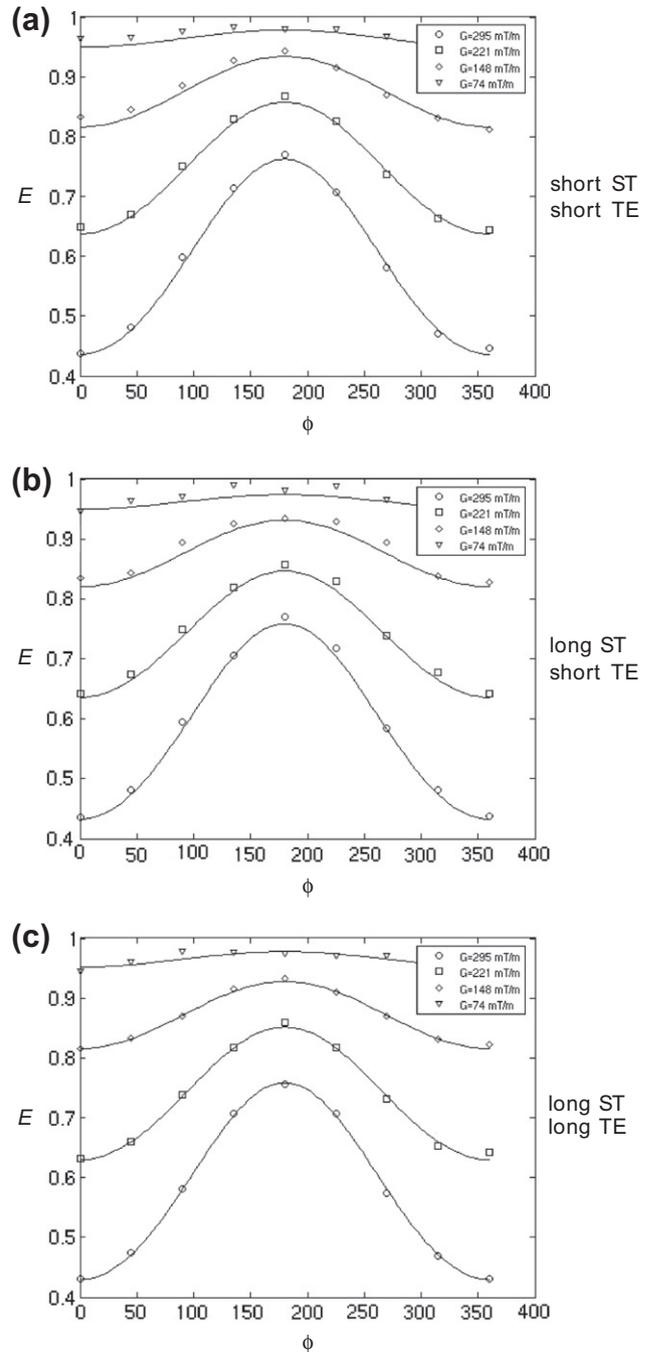
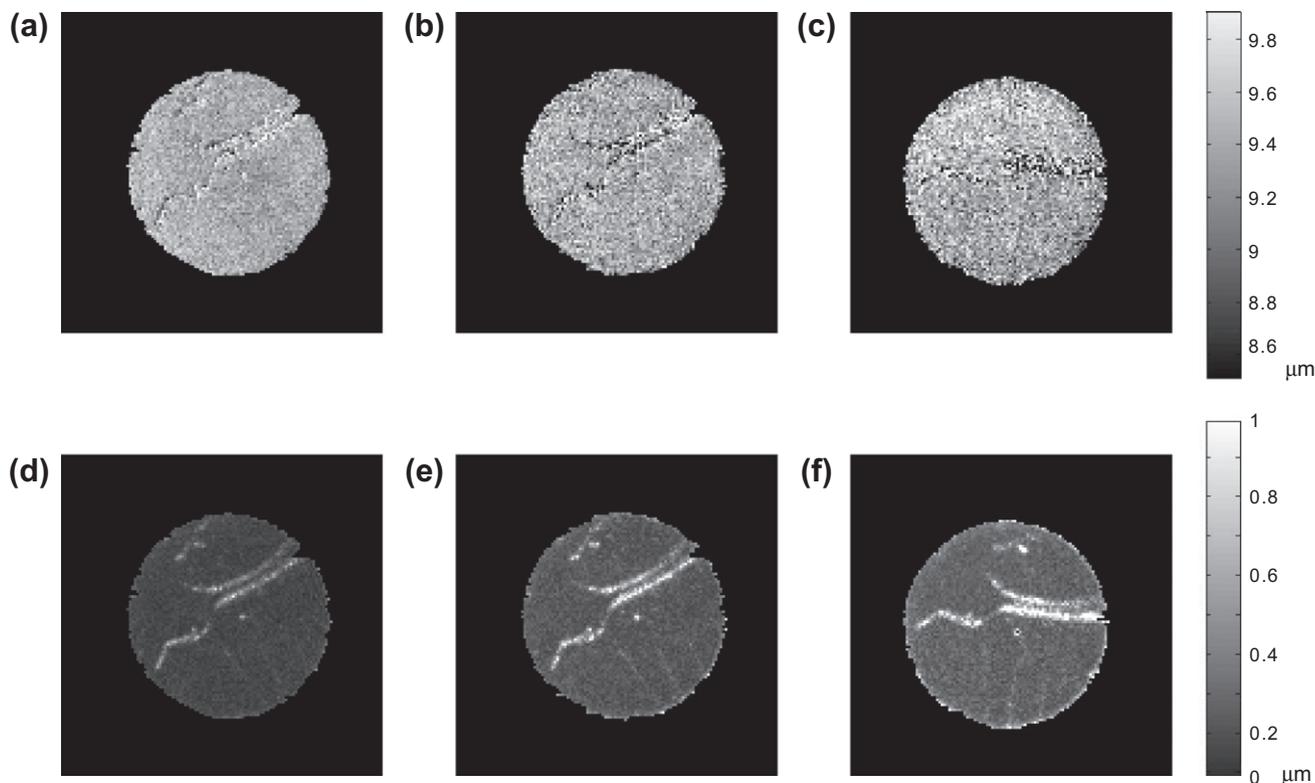


Fig. 5. Experimental and simulations of the corresponding echo attenuations vs.  $\phi$  for  $G = 0, 44, 74,$  and  $103 \text{ mT m}^{-1}$ . (a) TE = 12 ms and ST = 1.3 ms. (b) TE = 12 ms and ST = 20.8 ms. (c) TE = 70 ms and ST = 20.8 ms.

to the d-PFG MRI data presented in Fig. 4 and preserve all “anatomical” features of the sample. The uniform intensity throughout the image demonstrates a tight pore size distribution across the phantom. The standard deviation maps demonstrate the agreement between the theory and experimental data throughout the specimen.

Table 1 summarizes the pore diameter measurements corresponding to the three cases considered in Fig. 5 using three models: one in which the narrow gradient pulse regime was assumed, one which took into account all cross-terms and experimental parameters, and one that neglected the cross-term effects between diffusion and imaging gradients. The table presents the pore diameter estimations for all diffusion gradient strengths,



**Fig. 6.** Pore diameter map constructed from the d-PFG MRI data. (a) TE = 12 ms and ST = 1.3 ms. (b) TE = 12 ms and ST = 20.8 ms. (c) TE = 70 ms and ST = 20.8 ms and (d–f) show the corresponding standard deviations.

**Table 1**

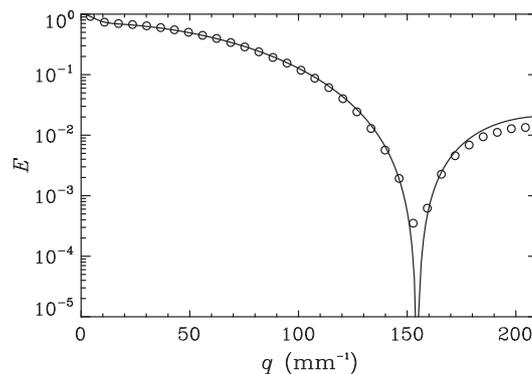
Pore diameter estimates of the GCA, all gradient strengths used in the experiment were incorporated into the simulations.

$d$ ( $\mu\text{m}$ )	Diffusion only	Diffusion + imaging	Narrow pulse approx
Short ST short TE	$9.44 \pm 0.03$	$9.41 \pm 0.03$	$7.00 \pm 0.05$
Long ST short TE	$9.45 \pm 0.02$	$9.45 \pm 0.02$	$7.00 \pm 0.04$
Long ST long TE	$9.47 \pm 0.02$	$9.47 \pm 0.02$	$7.05 \pm 0.06$

which consist of 38 data points in each simulation. The estimations based on the narrow pulse approximation yielded a considerably smaller pore diameter than the other two models (owing to motional narrowing [34]), which were very close to each other and within experimental error. However, a closer examination showed a small difference between the values determined by a model that took into account all imaging and diffusion gradients and one that neglected all imaging gradients for the shortest ST of 1.3 ms (Fig. 5a). For longer ST of 20.8 ms (Fig. 5b–c) there was no difference between the pore diameter values resulting from the simulations with and without incorporating the imaging gradients. In general one would consider the difference in pore diameter resulting from the short ST experiment (Fig. 5a) negligible as it is indeed within the experimental error of both our “golden standard” and the simulations. There is no way of telling which of the simulations is closer to the physical pore diameter; however, the small difference in those two simulations confirms that even when diffusion and imaging blocks are separated, if ST is shorter than the characteristic time it takes the spins to sample the pore ( $a^2/D_0$ , where  $a$  is the pore radius), imaging gradients should be incorporated into the simulations. This finding highlights the need to include *all* gradients appearing in the MRI sequence to obtain an accurate pore diameter estimate. This principle can be applied to any imaging

block concatenated to the d-PFG NMR block as long as those two block STs are sufficiently long the imaging gradient will not play a role in pore diameter determination.

Since in the GCA phantom, the capillaries are coherently organized, and monodisperse, and the GCA wafers themselves appear to be macroscopically homogeneous; diffusion–diffraction MR can be used as another way to measure pore diameter accurately. To further validate the findings from d-PFG filtered MRI we performed the diffusion–diffraction PFG measurements. Fig. 7 shows  $E$  vs.  $q$  plot for the PFG NMR experiment conducted in the direction perpendicular to the main axis of the GCA phantom’s pores. The diffraction minimum can be observed around  $q = 152 \text{ mm}^{-1}$ . It should be noted that a very similar signal decay manifesting a diffusion–diffraction minimum was observed in the  $y$ -direction (data not shown).



**Fig. 7.** Experiments and simulations of the echo attenuations vs.  $q$  for the PFG experiment using  $\delta = 4 \text{ ms}$ ,  $\Delta = 250 \text{ ms}$  and  $G_{\text{max}} = 1200 \text{ mT m}^{-1}$ .

The corresponding theoretical fit (solid line) for the  $E(q)$  data in the  $x$ -direction is superposed on the experimental points (symbols). Agreement is excellent. The pore diameter estimated from this diffraction pattern is  $9.35 \mu\text{m} \pm 0.05 \mu\text{m}$ . This provides another means to cross-validate the diameter measurements obtained using d-PFG MR methods.

#### 4. Discussion

The pore diameter estimates obtained from the d-PFG MRI experiments agree with those measured using light microscopy and PFG NMR experiments. This supports the claim that d-PFG MRI can provide accurate and precise estimates of pore diameter, albeit at a coarser length scale than optical microscopy. While optical microscopy here serves as a “gold standard” for comparing and contrasting our NMR and MRI findings, it is only viable when specimens are transparent, small, and thin. For materials that are optically turbid, thick or need to be studied at a large field of view (FOV), optical imaging methods become problematic. Since living biological tissue, and particularly human tissues and organs of interest are generally optically turbid, deep within the body, and large compared to an optical pixel or voxel, *in vivo* diffusion MRI microscopy remains the method of choice to perform *in situ* or *in vivo* histology.

Making d-PFG MRI quantitative, reproducible, and reliable requires that we ensure the integrity of our entire experimental and theoretical “pipeline.” In our case, this pipeline consists of novel filtered d-PFG MRI sequences, a general matrix operator-based mathematical modeling framework that predicts the signal attenuation produced by a d-PFG MRI pulse sequence in a restricted geometry, an efficient d-PFG MRI experimental design, MR data acquisition, and the estimation of microstructural features, like the local pore diameter, from this MRI data. Without a viable NMR and MRI phantom, validation of this pipeline is not possible, nor would one be possible to calibrate this experiment routinely for quality assurance purposes.

The GCA phantom used in this study is extremely appealing for a broad range of MRI applications since it consists of fused tubes where a substantial volume of each disk contains fluid. In the  $10 \mu\text{m}$  pore diameter phantom used in this study for example the center distance between adjacent pores is only  $12 \mu\text{m}$ . This arrangement provides greater pore volumes and thus, much more MR signal than an NMR phantom we have used previously, consisting of a pack of glass capillary tubes (Polymicro) in which pore volume represents only a very small fraction of the entire phantom volume. This additional signal might not be needed for NMR spectroscopy studies such as d-PFG NMR where using the same theoretical pipeline yielded accurate estimations of pore diameters at low  $q$ -values [13,35–37], however, it is essential to boost SNR in diffusion MRI experiments.

Since GCA wafers are available in various pore sizes and outer diameters, and are readily stacked or sandwiched together into more complex arrangements, we can, in principle, construct phantoms having a distribution of known pore sizes within individual voxels, which would be useful, for instance, in calibrating AxCaliber MRI [6].

The ultimate goal of this work is to develop and advance MRI methods for elucidating biologically and clinically important microstructural features in living tissue. Looking forward, as we begin to scan heterogeneous samples, including more complex phantoms, fixed and living tissues like skeletal muscle, spinal cord, and bundles of nerve axons all of whose diameter distributions may be spatially varying, we can expect the d-PFG MRI to yield quantitative maps that provide microstructural information that cannot be obtained by using other imaging methods.

#### 5. Summary

D-PFG MRI is a powerful tool for determining a variety of new and useful microstructural features within each voxel, which can be mapped or displayed in an imaging volume. We have successfully demonstrated that d-PFG-filtered MRI can measure and map the pore diameter in a novel glass capillary array phantom quantitatively. We also describe the development and use of a novel MRI phantom for calibrating and validating MRI measurements of pore diameter and diameter distribution.

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